

*Mathematical modeling, simulation  
optimization and control of crystallization  
processes for controlling the particulate  
properties*

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# Outline

PhD objectives: a short presentation of the main purposes of the thesis



The main results of the first part of PhD summarizing the main results

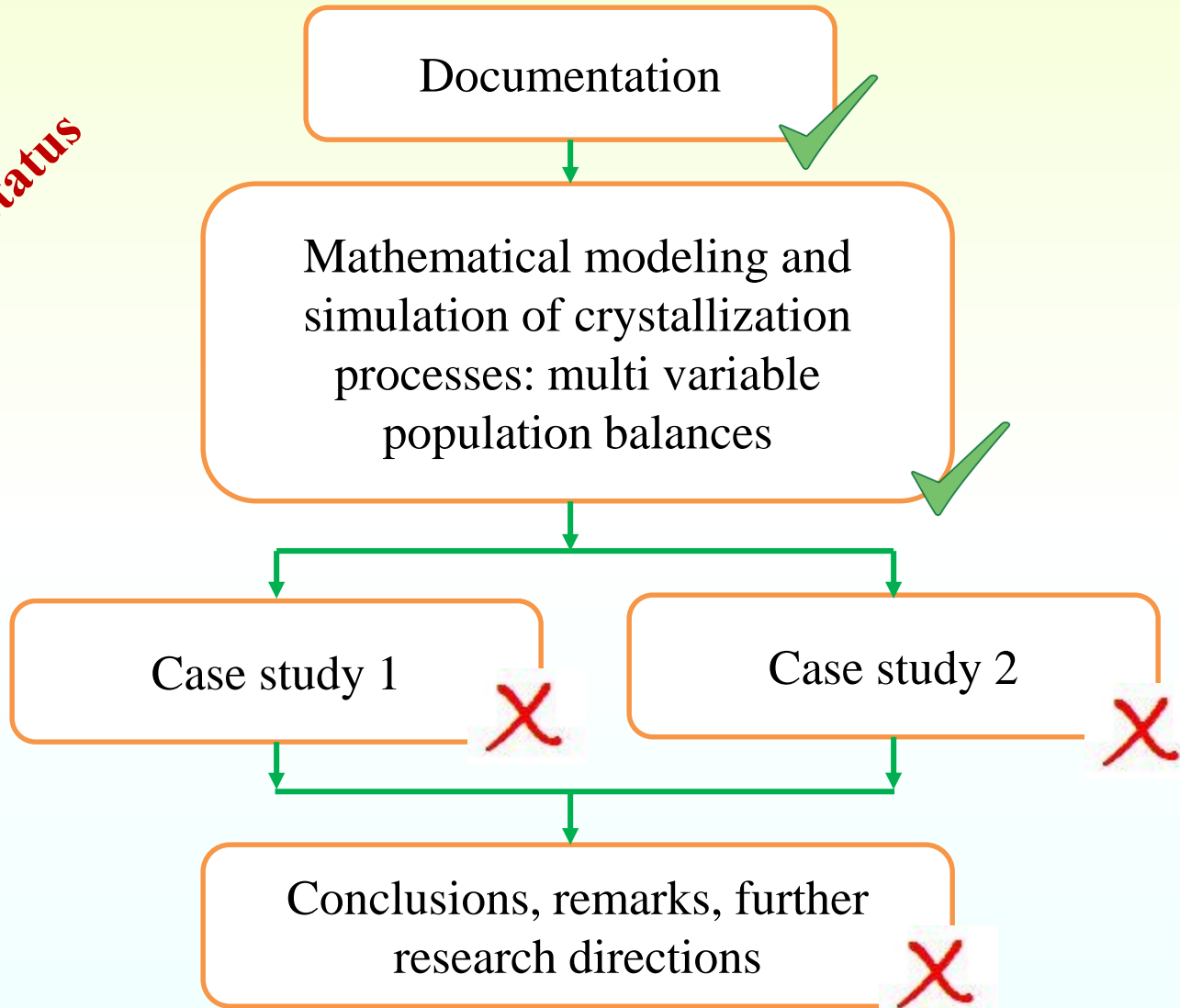


Future plans  
??



# PhD objectives

*Current status*



# M-PB: Crystallization of plate-like crystals

- **Phenomenon of plate-like particle crystallization**

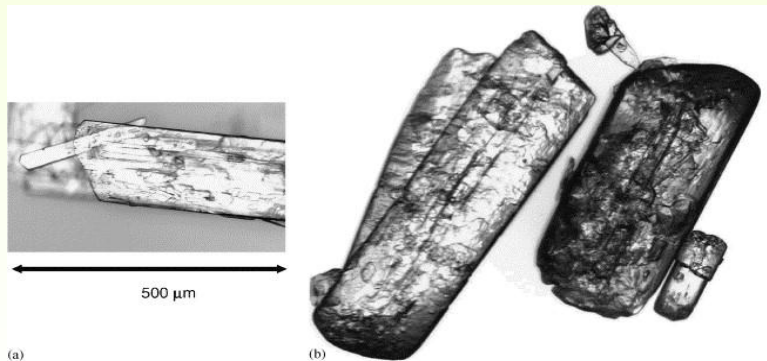


Figure 1. Plate like crystal [1]

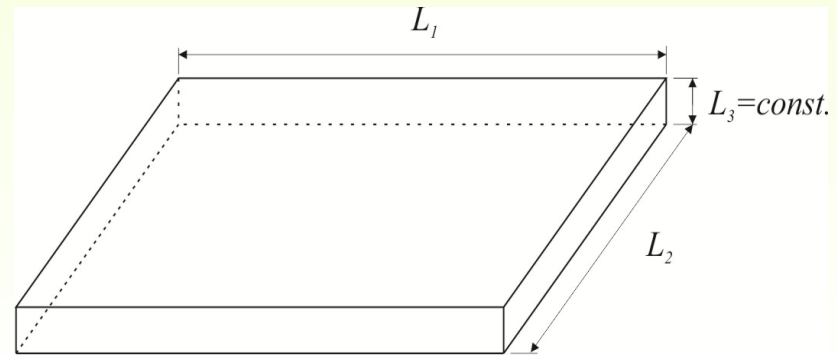


Figure 2. Plate like crystal shape [2]

- **Mathematical model (the population balance only)**

$$\frac{\partial n(L_1, L_2, t)}{\partial t} + \frac{\partial [G_1 n(L_1, L_2, t)]}{\partial L_1} + \frac{\partial [G_2 n(L_1, L_2, t)]}{\partial L_2} = B(L_1, L_2, t)$$

With the appropriate initial and boundary conditions

# M-PB: Crystallization of plate-like crystals

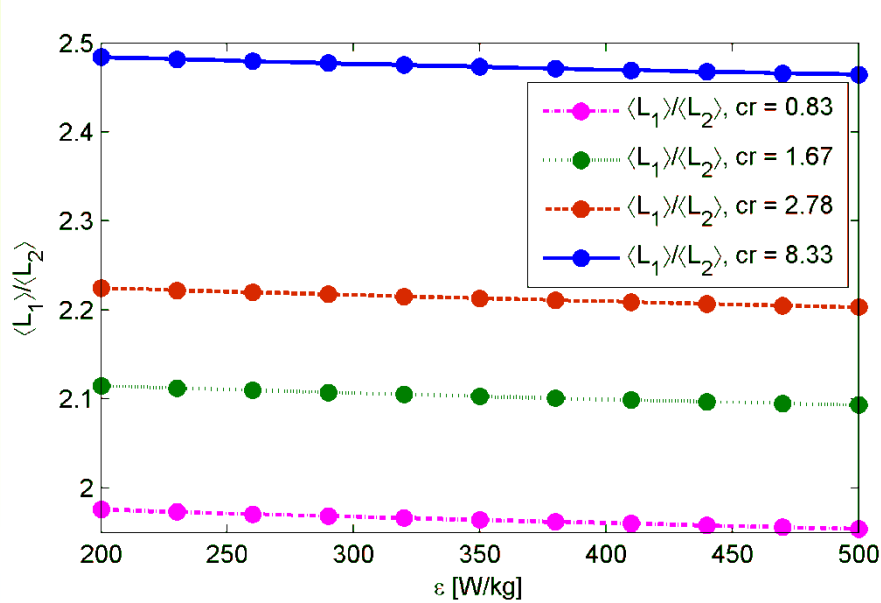


Figure 3. Effects of cooling rate on particle shape [2]

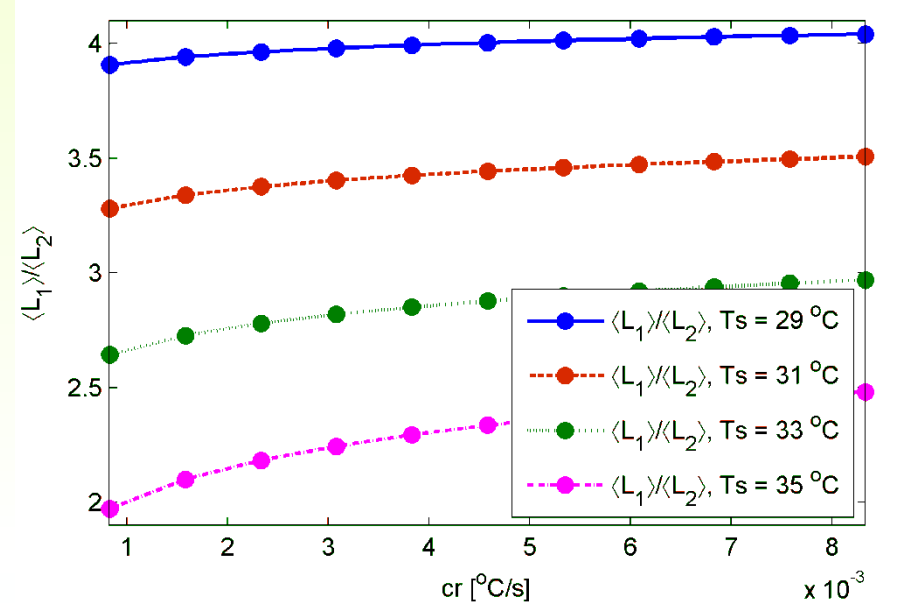


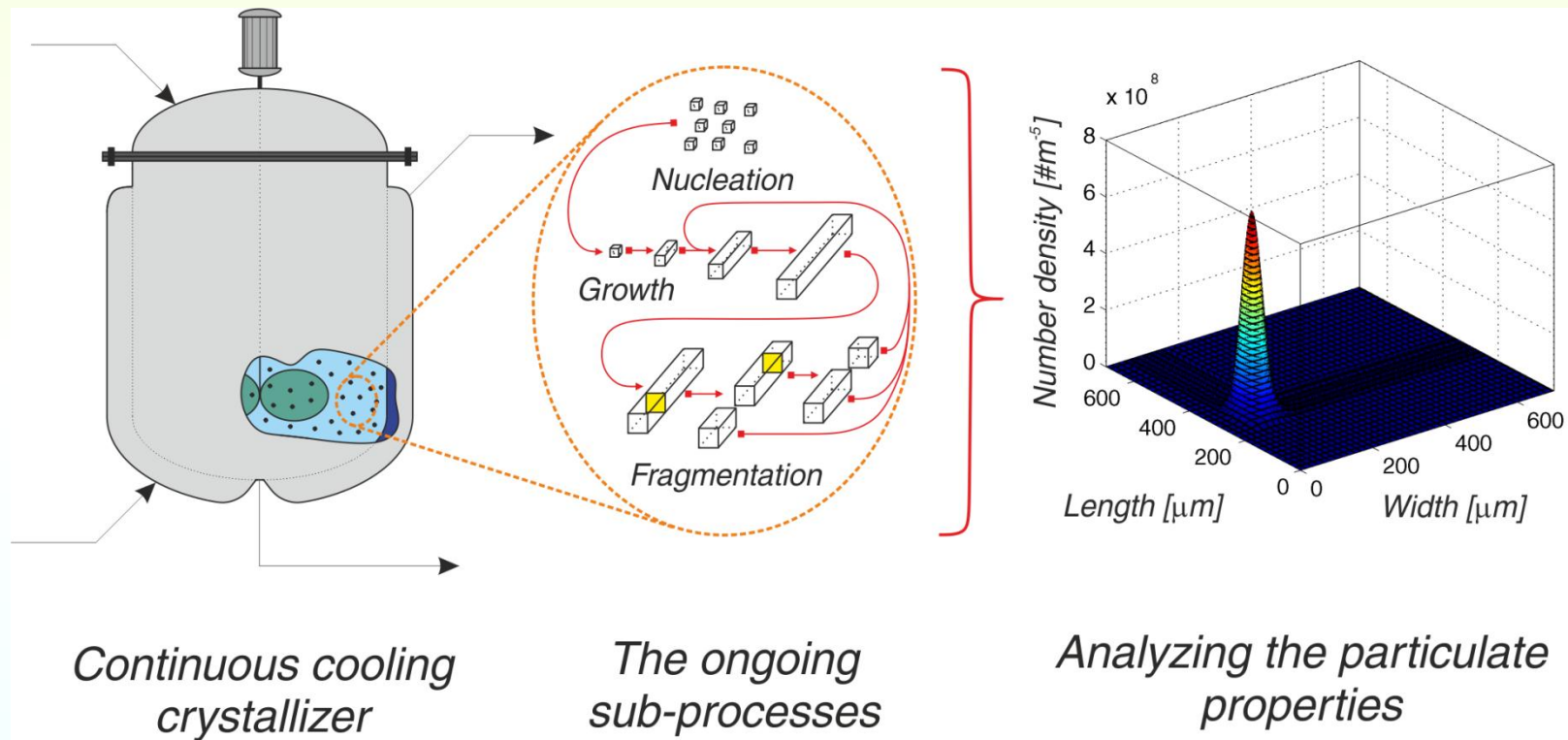
Figure 4. Effects of seeding temperature on particle shape [2]



Figure 5. Realizable interval of particle shape

# M-PB: Crystallization of rod-like crystals

- *Phenomenon of rod-like particle crystallization*



**Figure 6.** The rod-like particle crystallization

# M-PB: Rod like crystallization: A “simple” PB model

- **Mathematical model (the population balance only)**

$$\begin{aligned} \frac{\partial n(L_1, L_2, t)}{\partial t} + \frac{\partial [G_1 n(L_1, L_2, t)]}{\partial L_1} + \frac{\partial [G_2 n(L_1, L_2, t)]}{\partial L_2} &= \frac{1}{\tau} [n_{in}(L_1, L_2, t) - n(L_1, L_2, t)] \\ + B_p(t) \delta(L_1 - L_n, L_2 - L_n) - k_{br} \int_0^{L_m} \int_0^{L_m} b_{br}^1(\lambda_1, L_1) b_{br}^2(\lambda_2, L_2) L_1^\beta L_2^\gamma n(L_1, L_2, t) d\lambda_1 d\lambda_2 \\ + k_{br} \int_0^{L_m} \int_0^{L_m} b_{br}^1(L_1, \lambda_1) b_{br}^2(L_2, \lambda_2) \lambda_1^\beta \lambda_2^\gamma n(\lambda_1, \lambda_2, t) d\lambda_1 d\lambda_2 \end{aligned}$$

With the appropriate initial and boundary conditions

- +++ Kinetic equations for primary nucleation, growth and particle-impeller collision breakage
- +++ Heat and mass balance equations
- +++ Solution of model-equations

# Conclusions

- *In the last months 1 article was accepted in an ISI indexed journal – Periodica Polytechnica – Chemical Engineering and*
- *In the last months 1 article was submitted to an ISI indexed journal – Powder Technology*
- *Future plans (for the following 2 months):*
  - *Finalize the codes and write the manuscript for the 2D finite volume PBE solution*
  - *Prepare the simulation data for the heat effect manuscript*



***Thank you for your attention!***